

- Adjacencies(g)
- VertexDegrees(g)
- Edges(g)
- CompletesOfGivenOrder(g,o)
- ConnectedComponents(g)
- GraphAttributeStatistics(n,p,F) Returns information about the parameter F for 100 random graphs of order  $n$  and edge probability  $p$ .
- BoundaryVertices(g) For  $g$  a triangulation of a compact surface, returns the list of vertices whose link is isomorphic to a path.
- InteriorVertices(g)
- SpanningForestEdges(g)

Distances

- Distance(g,x,y)
- DistanceMatrix(g)
- Diameter(g)
- Eccentricity(g,x)
- Radius(g)
- Distances(g,a,b)  $a, b$  are lists of vertices. Returns a list.
- DistanceSet(g,a,b) As before, but returns a set.
- DistanceGraph(g,d) The graph with vertex set the vertices of  $g$ , two vertices adjacent if their distance is in  $d$ .
- PowerGraph(g,n) Same as the distance graph with set of distance  $\{1, \dots, n\}$ .

Graph morphisms

- IsoMorphisms(g,h)

- AutomorphismGroup(g)
- Morphism(g,h), Morphisms(g,h), NextMorphism(g,h,f)
- MonoMorphism(g,h), MonoMorphisms(g,h), NextMonoMorphism(g,h,f)
- EpiMorphism(g,h), EpiMorphisms(g,h), NextEpiMorphism(g,h,f)
- WeakMorphism(g,h), WeakMorphisms(g,h), NextWeakMorphism(g,h,f), and more predefined classes of morphisms and the possibility to define new classes

Small Graphs

- ConnectedGraphsOfGivenOrder(n) Up to  $n = 9$ .
- Graph6ToGraph(s)  $s$  is a string.
- GraphsOfGivenOrder(n) Up to  $n = 9$ .
- ImportGraph6(f)  $f$  is a filename.

Graph categories

- DefaultGraphCategory A variable that holds the current graph category. Has to be set with, e.g. SetDefaultCategory(OrientedGraphs)

Graph categories:

Graphs, UndirectedGraphs, LooplessGraphs, SimpleGraphs, OrientedGraphs.

Digraphs

- InNeigh(g,x) List of in-neighbors of  $x$  in  $g$ .
- IsTournament(g)
- IsTransitiveTournament(g)

- Orientations(g) List of all oriented graphs that can be obtained from  $g$

Draw

- Draw(g) Shows a window with a drawing of  $g$ . Commands in the draw window: h:help, f:fit graph, l: toggle labels, d: toggle dynamics, r: toggle repulsion, s: save & quit, q: quit without saving

Backtrack

Example: coloring with two colors:

```
g:=PathGraph(3);
chk:=function(L,g)
  local x,y;
  if L=[] then return true; fi;
  x:=Length(L);
  for y in [1..x-1] do
    if IsEdge(g,[x,y]) and L[x]=L[y] then
      return false;
    fi;
  od;
  return true;
end;

then BacktrackBag([0,1],chk,Order(g),g); returns [ [ 0, 1, 0 ],
[ 1, 0, 1 ] ].
```